## Study guide for additional concepts - Pre-calc/alg review

Factor out the lowest exponent and simplify:

$$x^{1/2} - x^{5/2}$$

$$x^{-1/2}(x+3)^{1/2} + x^{1/2}(x+3)^{-1/2}$$

$$x^{3/2} + 8x^{1/2} + 15x^{-1/2}$$

$$4(x+1)^{1/2} - 5(x+1)^{3/2} + (x+1)^{5/2}$$

$$2x^{1/2} + 5x^{-1/2} + 2x^{-3/2}$$

$$(x+2)^{7/2} - (x+2)^{3/2}$$

$$(x^3+2)^{1/3}+(x^3+2)^{-5/3}$$

$$\frac{2x(4x+7)^{1/3} - \frac{4}{3}x^2(4x+7)^{-2/3}}{(4x+7)^{2/3}}$$

For each function, find the equations of both the vertical asymptote(s) and horizontal asymptotes (if they exist)

1.) 
$$y = \frac{x}{x-3}$$

2.) 
$$y = \frac{x+4}{x^2+1}$$

3.) 
$$y = \frac{x^2 - 9}{x^3 + 3x^2 - 18x}$$

4.) 
$$y = \frac{2x^2 + 6x}{x^3 - 3x^2 - 4x}$$

5.) 
$$y = \frac{\sqrt{x}}{2x^2 - 10}$$

Find the oblique asymptote using long division. Also state any vertical asymptotes/holes.

$$f(x) = \frac{x^2 - 6x - 1}{x + 3}$$

$$f(x) = \frac{x^2 + 6x - 4}{3x - 6}$$

$$f(x) = \frac{x^3 - 5x}{x^2 + 1}$$

$$f(x) = \frac{x^2 + 2x - 12}{x - 5}$$

$$f(x) = \frac{3x^3}{4x^2 - 8x}$$